



POLYTECHNIQUE

# A REVIEW FOR BENCHMARK EXPERIMENTS FOR VALIDATION OF PERIDYNAMIC MODELS

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# **MOTIVATION**

#### Adequacy of peridynamic models and simulations

One important key for the adequacy of a model is the confidence how it compares with experimental data [27, 28].

#### Main objectives

- · Review the available experimental data
- Provide an measurement for the confidence level
- Advanced visualization techniques for additional comparison against experiments



#### Methodology

Comparison against experiments

Confidence of peridynamics models and simulations

Advanced visualization techniques

Conclusion and Outlook

## OUTLINE



## Methodology

- Collection of data
- Metric for the comparison

## **2** Comparison against experiments

- Wave propagation
- Crack initiation/propagation Composite
  Steel/Aluminum
  Concrete
  Glass
  Various

# **3** Confidence of peridynamics models and

#### SIMULATIONS

- Scalar observable
- Series of obversable

## Advanced visualization techniques

- Physically-based rendering
  - Extraction of additional attributes

# **5** Conclusion and Outlook



#### Methodology

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## **COLLECTION OF DATA**

Search in Web of Science<sup>1</sup> for

**Comparison against experiments** 

- peridynamics + experiment
- peridynamics + benchmark
- · 39 papers including comparison against experimental data
- Using 52 experimental paper

#### Advanced visualization techniques

- peridynamics + computer graphics
- peridynamics + visualization
- 5 papers (2 physically-based rendering and 3 for the extraction)
- Using 1 experimental paper



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<sup>&</sup>lt;sup>1</sup>https://webofknowledge.com/

## METRIC FOR COMPARISON OF EXPERIMENTAL DATA





#### Methodology Collection of data

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# $R^2 \in [0, 1]$ correlation

- Obtain y-values from simulation and y-values from experiment at same x-values
- Do linear regression with y-values
- Use *r* value squared as confidence level

## **COMPARISON OF WAVE PROPAGATION AGAINST EXPERIMENTS**

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| Application                            | В            | S            | Material                | Exp          |
|--|--------------|--------------|-------------------------|--------------|
| Stress wave propagation (half-plane)   | $\checkmark$ |              | Plastic polymer (CR-39) | [20]         |
| Wave speed (Edge-on impact experiment) | $\checkmark$ |              | ALON, PMMA              | [76, 75, 74] |
| Split-Hopkinson pressure bar           | $\checkmark$ |              | Aluminum                | [17, 10]     |
| Wave dispersion and propagation        |              | $\checkmark$ | Sandstone               | [82, 89]     |

Table 1: Applications for the comparison of wave propagation against experimental resuls. Legend: B refers to bond-based peridynamics, S refers to state-based peridynamics, Exp to experimental data, and Sim to simulation.

# COMPOSITE

| Application  | В            | s | Material  | Exp            | Sim  |
|--|--------------|---|-----------|----------------|------|
| Interaction between a dynamically growing crack      | $\checkmark$ |   | Composite | [53]           | [2]  |
| Damage growth prediction (Six-bolt specimen)         | $\checkmark$ |   | Composite | [73]           | [64] |
| Damage prediction (Center-cracked laminates)         | $\checkmark$ |   | Composite | [4, 48, 83, 8] | [49] |
| Dynamic tension test (prenoteched rectangular plate) | $\checkmark$ |   | Composite | [43, 8]        | [39] |

Table 2: Applications of bond-based and state-based peridynamics for the comparison with experimental data. **Legend: B** refers to bond-based peridynamics, **S** refers to state-based peridynamics, **Exp** to experimental data, and **Sim** to simulation.

- Only quantitative comparison against experiment was done, e.g. crack pattern or crack branches.
- Only bond-based peridynamic models were applied.

# **STEEL/ALUMINUM**

| Application                     | В            | S            | Material           | Exp             | Sim             |
|---------------------------------|--------------|--------------|--------------------|-----------------|-----------------|
| Crack growth (Kalthoff-Winkler) | $\checkmark$ | $\checkmark$ | Steel              | [45, 47, 46]    | [71, 3, 36, 90] |
| Dynamic fracture                |              | $\checkmark$ | Steel (4340)       | [32]            | [31]            |
| Fracture (Compact tension test) | $\checkmark$ |              | Aluminum,Steel     | [59, 61, 7, 54] | [84, 88, 87]    |
| Taylor impact test              |              | $\checkmark$ | Aluminum           | [16, 44]        | [29, 30, 3]     |
| Ballistic impact test           |              | $\checkmark$ | Aluminum (6061-T6) | [81]            | [79]            |

Table 3: Applications of bond-based and state-based peridynamics for the comparison with experimental data. Legend: B refers to bond-based peridynamics, S refers to state-based peridynamics, Exp to experimental data, and Sim to simulation.

## **CONCRETE**

| Application   | В      | s      | Material                         | Exp                      | Sim                     |
|---|--------|--------|----------------------------------|--------------------------|-------------------------|
| Lap-splice experiment<br>3-point bending beam<br>Failure in a Barazilian disk under compression | √<br>√ | √<br>√ | Concrete<br>Concrete<br>Concrete | [33]<br>[41, 14]<br>[35] | [33]<br>[35, 5]<br>[38] |

Table 4: Applications of bond-based and state-based peridynamics for the comparison with experimental data. **Legend: B** refers to bond-based peridynamics, **S** refers to state-based peridynamics, **Exp** to experimental data, and **Sim** to simulation.

# GLASS

| Application  | В                        | S | Material  | Exp  | Sim  |
|--|--------------------------|---|---|--|--|
| Dynamic crack propagation (prenotched thin plate)<br>Impact damage with a thin polycarbonate backing<br>Single crack paths (quenched glass plate)<br>Multiple crack paths (quenched glass plate)<br>Crack tip propagation speed<br>Fast cracks in PMMA | <b>\$ \$ \$ \$ \$ \$</b> |   | Glass<br>Glass<br>Glass<br>Glass<br>Glass<br>PMMA | [11, 24, 67]<br>[26, 15, 6]<br>[86, 69, 9]<br>[70, 85]<br>[11]<br>[25] | [90, 37, 2]<br>[40]<br>[50]<br>[50]<br>[36, 90, 37]<br>[2] |
| Tensile test   | $\checkmark$             |   | PMMA  | [77]   | [21]   |

Table 5: Applications of bond-based and state-based peridynamics for the comparison with experimental data. Legend: B refers to bond-based peridynamics, S refers to state-based peridynamics, Exp to experimental data, and Sim to simulation.

- Six papers comapred against the same experimental results: FP Bowden et al. "Controlled fracture of brittle solids and interruption of electrical current". In: *Nature* 216.5110 (1967), pp. 38–42.
- Only bond-based peridynamics was considered.

## VARIOUS

| Application               | В            | S            | Material                    | Exp         | Sim  |
|---------------------------|--------------|--------------|-----------------------------|-------------|------|
| Ruptures in Bio membranes |              | $\checkmark$ | Bio membranes               | [34]        | [78] |
| Arctic engineering        |              | $\checkmark$ | Ice                         | [72]        | [57] |
| Electronic packages       | $\checkmark$ |              | Graphene                    | [63]        | [65] |
| Dynamic crack propagation | $\checkmark$ |              | FGM (Epoxy/Soda-lime glass) | [51, 1, 52] | [19] |

Table 6: Applications of bond-based and state-based peridynamics for the comparison with experimental data. Legend: B refers to bond-based peridynamics, S refers to state-based peridynamics, Exp to experimental data, and Sim to simulation.

- For arctic engineering three different speeds of the drill were compared.
- Confidence level heavily depends on the speed value.

## **R**ELATIVE ERROR FOR SCALAR OBSERVABLE



Figure 1: The plot shows the relation between the Young modulus *E* of the material and the relative error of the experimental result and the obtained observable in the simulation.

Table

Relative error



## **OVERVIEW RELATIVE ERROR**

| Application                                 | Material  | Observable                                   | Rel. error            | Exp      | Sim  |
|---|-----------|--|-----------------------|----------|------|
| Edge-on impact experiment                   | ALON      | Avg. propagation speed of primary wave front | $3.57 \cdot 10^{-2}$  | [60]     | [87] |
| Kalthoff-Winkler experiment                 | Steel     | Crack initiation time                        | $-3.45 \cdot 10^{-2}$ | [58]     | [36] |
| Kalthoff-Winkler experiment                 | Steel     | Crack propagation speed                      | 0.14                  | [45, 68] | [12] |
| Crushing-brittle ice by a rotating cylinder | Ice       | Mean force at 50 mm s <sup>-1</sup>          | -0.74                 | [72]     | [57] |
| Crushing-brittle ice by a rotating cylinder | Ice       | Mean force at 130 mm s <sup>-1</sup>         | -0.21                 | [72]     | [57] |
| Crushing-brittle ice by a rotating cylinder | Ice       | Mean force at 210 mm s <sup>-1</sup>         | -0.25                 | [72]     | [57] |
| Crushing-brittle ice by a rotating cylinder | Ice       | Peak force at 50 mm s <sup>-1</sup>          | -0.66                 | [72]     | [57] |
| Crushing-brittle ice by a rotating cylinder | Ice       | Peak force at 130 mm s <sup>-1</sup>         | -0.12                 | [72]     | [57] |
| Crushing-brittle ice by a rotating cylinder | Ice       | Peak force at 210 mm s <sup>-1</sup>         | 0.29                  | [72]     | [57] |
| Pre-cracked glass (step tensile loading)    | Soda-lime | Max. crack propagation speed                 | $6.27 \cdot 10^{-2}$  | [11]     | [37] |
| Pre-cracked plate (step tensile loading)    | Soda-lime | Max. crack propagation speed                 | -0.27                 | [11]     | [90] |
| Pre-cracked plate (step tensile loading)    | Soda-lime | Max. crack propagation speed (16 281 nodes)  | 0.29                  | [11]     | [36] |
| Pre-cracked plate (step tensile loading)    | Soda-lime | Max. crack propagation speed (4141 nodes)    | 0.48                  | [11]     | [36] |
| Pre-cracked plate (step tensile loading)    | Soda-lime | Max. crack propagation speed (refined)       | 0.71                  | [11]     | [36] |

Table 7: Relative error between the observable measured in the experiment and obtained in the simulation.

# $R^2$ correlation for series of observable



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Scalar observable

#### Series of obversable

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Figure 2: The plot shows the relation between the Young modulus *E* of the material and the extracted correlation  $R^2$  of the experimental plot and the plot obtained by simulations.

Table

# **OVERVIEW** R<sup>2</sup> CORRELATION

| Application                     | Material                    | Observable                             | R <sup>2</sup> | Exp      | Sim  |
|---------------------------------|-----------------------------|--|----------------|----------|------|
| Split-Hopkinson pressure bar    | Aluminum                    | Strain vs time                         | 0.99           | [17]     | [42] |
| Taylor impact test              | Aluminum (6061-T6)          | Norm diameter/length; strain vs stress | 0.96           | [44, 16] | [29] |
| Ballistic impact test           | Aluminum (6061-T6)          | Residual vel vs impact vel             | 0.99           | [81]     | [79] |
| Dynamic fracture                | Steel (4340)                | Strain vs stress                       | 0.97           | [32]     | [31] |
| Compact tension test            | Aluminum (D16AT)            | Force vs CMOD                          | 1              | [54, 80] | [84] |
| Compact tension test            | SAE 1020 steel              | Crack path position                    | 0.97           | [61]     | [87] |
| 3-point bending                 | Concrete                    | Load vs CMD                            | 0.61           | [41]     | [35] |
| 3-point bending (D3)            | Concrete                    | Load vs CMOD                           | 0.85           | [14]     | [5]  |
| 3-point bending (D6)            | Concrete                    | Load vs CMOD                           | 0.89           | [14]     | [5]  |
| 3-point bending (D9)            | Concrete                    | Load vs CMOD                           | 0.77           | [14]     | [5]  |
| 3-point bending (D3 LPD-load)   | Concrete                    | Load vs LPD                            | 0.87           | [14]     | [5]  |
| 3-point bending (D6 LPD-load)   | Concrete                    | Load vs LPD                            | 0.83           | [14]     | [5]  |
| 3-point bending (D9 LPD-load)   | Concrete                    | Load vs LPD                            | 0.51           | [14]     | [5]  |
| Fast crack growth               | PMMA                        | Crack velocity vs time                 | 0.72           | [25]     | [2]  |
| Tensile test                    | PMMA                        | Poisson ratio vs time                  | 0.65           | [77]     | [21] |
| 3-point loading                 | FEM (Epoxy/Soda-lime glass) | Crack length vs time                   | 0.99           | [52]     | [19] |
| Wave dispersion and propagation | Sandstone                   | Dispersion curves                      | 0.93           | [82]     | [13] |

Table 8:  $R^2$  correlation between the series of observables between experiment and simulation. **Abbreviations**: crack mouth displacement (CMD), crack mouth opening displacement (CMOD), and load point displacement (LPD).

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## **PHYSICALLY-BASED RENDERING**





Wei Chen et al. "Peridynamics-Based Fracture Animation for Elastoplastic Solids". In: *Computer Graphics Forum* (2017), n/a–n/a. ISSN: 1467-8659



J. A. Levine et al. "A Peridynamic Perspective on Spring-mass Fracture". In: Proceedings of the ACM SIGGRAPH/Eurographics Symposium on Computer Animation. SCA '14. Copenhagen, Denmark: Eurographics Association, 2014, pp. 47–55

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## **EXTRACTION OF FRAGMENTS**







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- David Littlewood, Stewart Silling, and Paul Demmie. "Identification of Fragments in a Meshfree Peridynamic Simulation". In: ASME 2016 International Mechanical Engineering Congress and Exposition. American Society of Mechanical Engineers. 2016, V009T12A071–V009T12A071
- Patrick Diehl et al. "Extraction of Fragments and Waves After Impact Damage in Particle-Based Simulations". In: Meshfree Methods for Partial Differential Equations VIII. Springer International Publishing, 2017, pp. 17–34

## **FRACTURE PROGRESSION**



|  |           |                                       | Comparison aga<br>experiments                      |
|--|-----------|---------------------------------------|--|
|  | Setting   | Growth velocity $m s^{-1}$            | Confidence of<br>peridynamics m<br>and simulations |
| Veixing<br>65/her52                          | Exp       | 1000                                  | Advanced<br>visualization<br>techniques            |
| A1726-02<br>27856-02<br>27856-02<br>27856-02 | SPH<br>PD | 1200<br>Mean: 1142 Median: 1144       | Physically-base<br>rendering                       |
|  | I D       | 1 $1$ $1$ $1$ $1$ $1$ $1$ $1$ $1$ $1$ | Estra ation of                                     |

Michael Bußler et al. "Visualization of fracture progression in peridynamics". In: Computers & Graphics 67 (2017), pp. 45–57. ISSN: 0097-8493

Extraction of additional attributes

## **SUMMARY**



Methodology

Comparison against experiments

Confidence of peridynamics models and simulations

Advanced visualization techniques

Physically-based rendering

Extraction of additional attributes

Conclusion and Outlook

References

| Application                                | В            | S            | Reference |
|--|--------------|--------------|-----------|
| Animation of brittle fracture              | $\checkmark$ |              | [55]      |
| Fracture animation in elastoplastic solids |              | $\checkmark$ | [18]      |
| Waves after impact damage                  | $\checkmark$ |              | [23]      |
| Fracture progression                       | $\checkmark$ | $\checkmark$ | [12]      |
| Extraction of fragments                    | $\checkmark$ |              | [23, 56]  |

Table 9: Overview of applications of bond-based and state-based peridynamics in visualization of fracture in solids. **Legend**: *B* refers to bond-based peridynamics and *S* refers to state-based peridynamics.

- All these advances techniques are additional models.
- Validation against experiments is needed for these models.