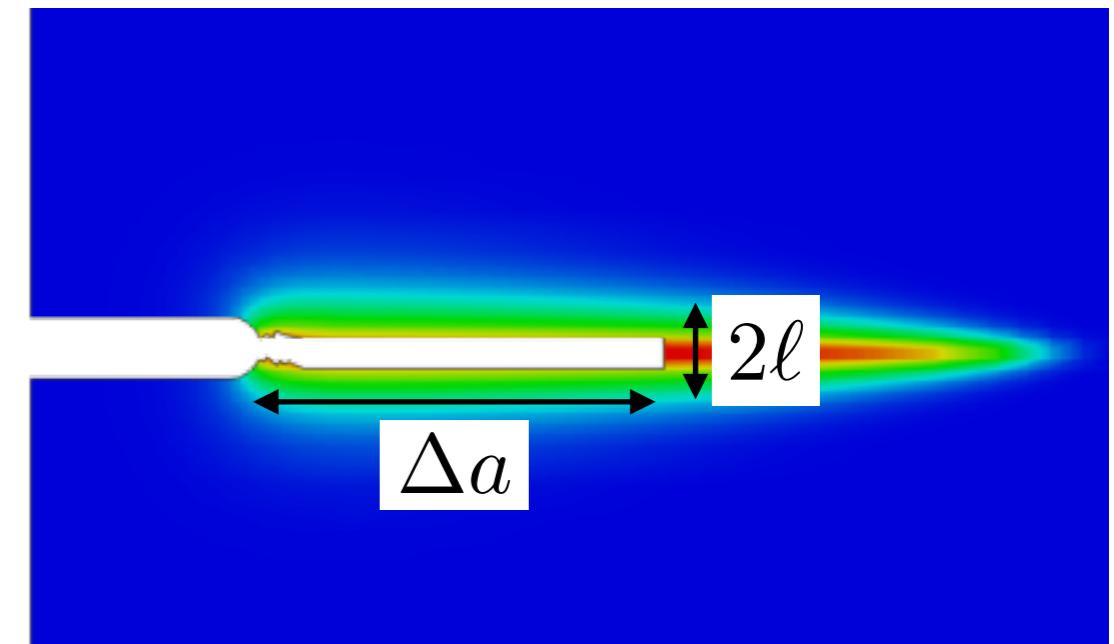
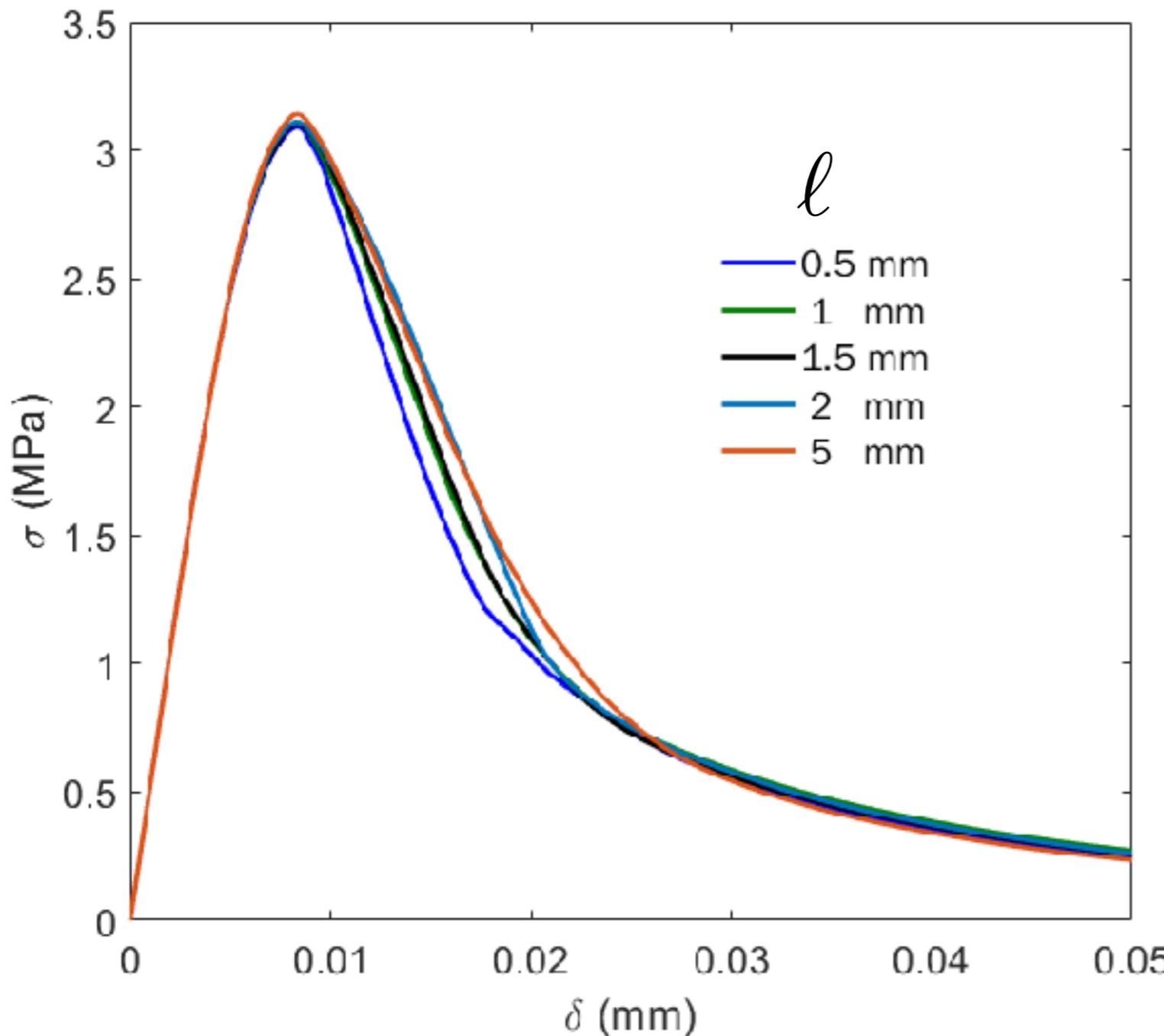


# Sensitivity to change in the length scale



- Energy dissipated in the shown volume  
 $\propto \psi_* \ell \Delta a$
- The energy dissipated per unit surface area of crack extension  
 $\propto \psi_* \ell$

$$\psi_* \ell = \text{constant}$$

# 3-Pt Bend tests of Bazant and co-workers



## Comprehensive concrete fracture tests: Description and results



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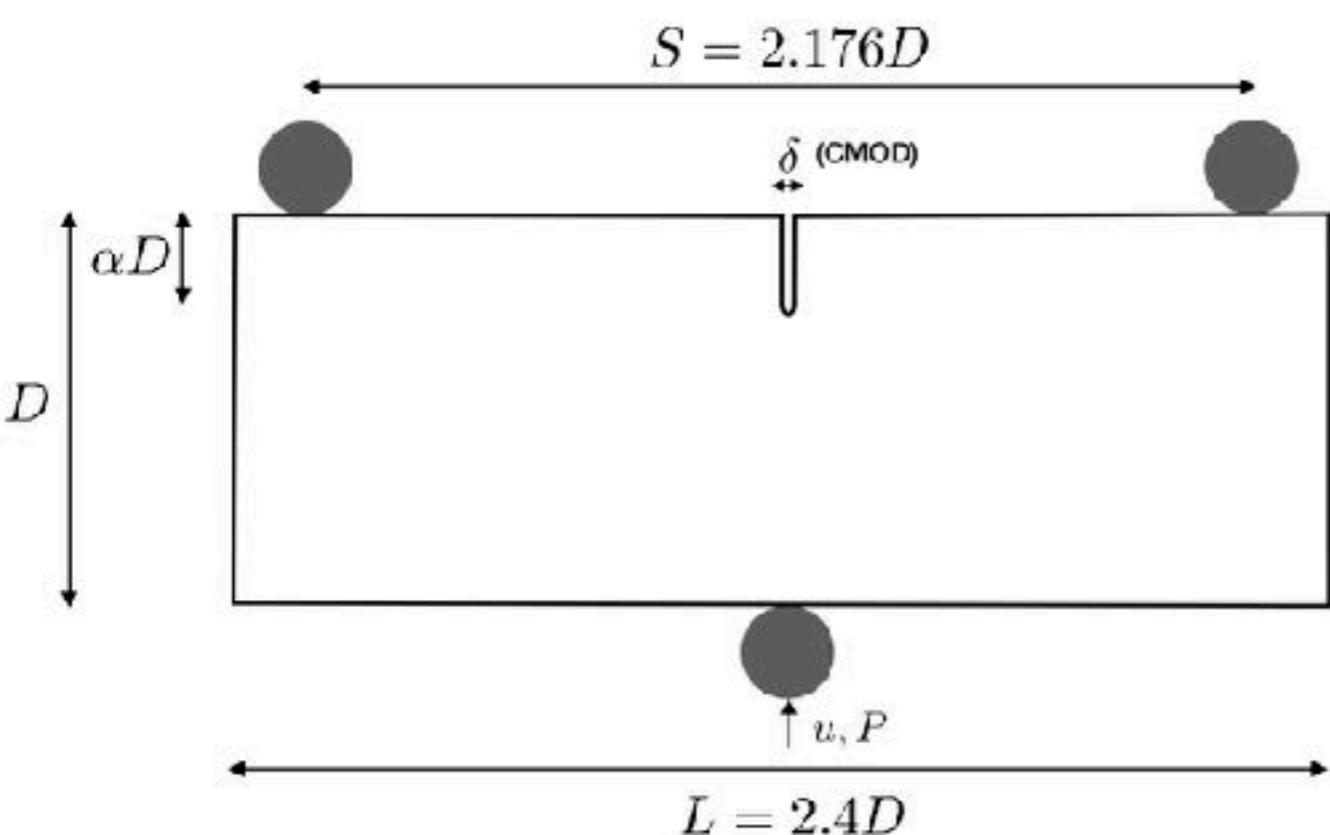
### ABSTRACT

Although hundreds of concrete fracture tests exist, their evaluation is ambiguous because they have limited ranges of specimen size, initial notch depth and postpeak response, and refer to different concretes, different batches of concrete, different ages, different environmental conditions, different loading rates and test procedures, and different specimen types. Presented is an experimental investigation of unprecedented comprehensiveness and low scatter, using specimens made from one batch of concrete. It includes: (1) notched and unnotched beams tested at virtually the same age; (2) crack depths ranging from 0% to 30% of beam depth; (3) a broad size range (1: 12.5); (4) tests in transition between type 1 and type 2 size effects; (5) virtually complete postpeak softening data; (6) properly correlated loading rates; and (7) complete standard characterization of the concrete used. The analysis is relegated to a follow-up paper.

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- Multi-million experimental research effort on concrete funded by DOT in 2013, to obtain pedigreed data from a single batch of concrete.

# 3-Pt Bend tests of Bazant and co-workers

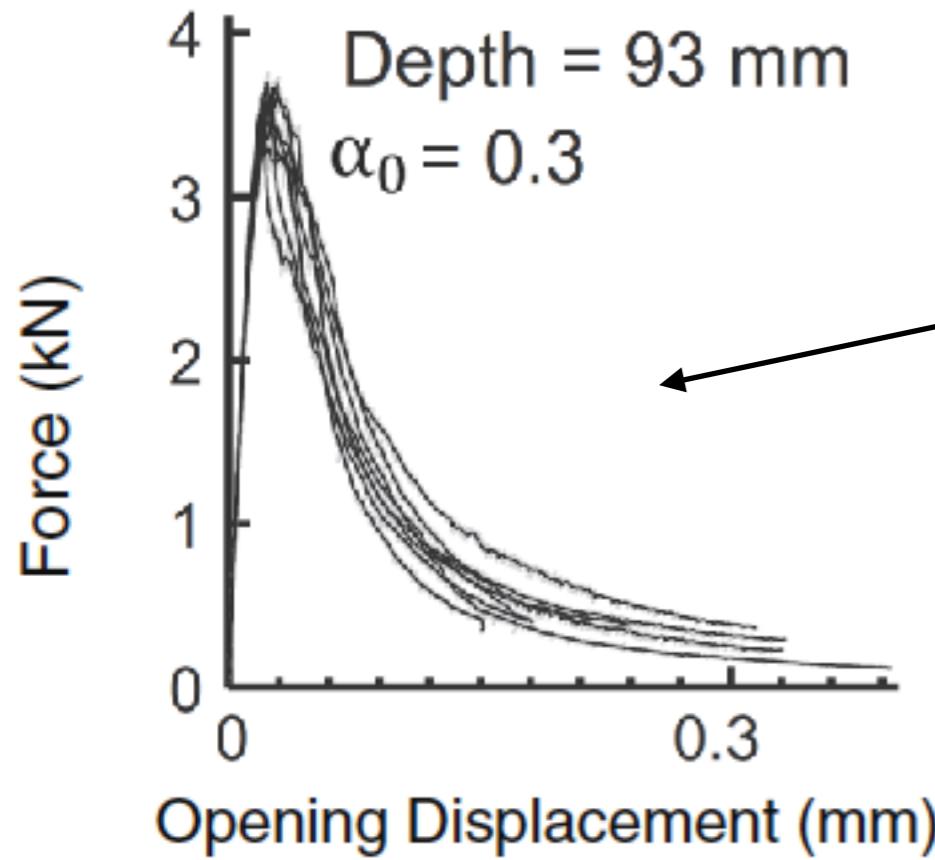


Thickness of specimens: 40 mm

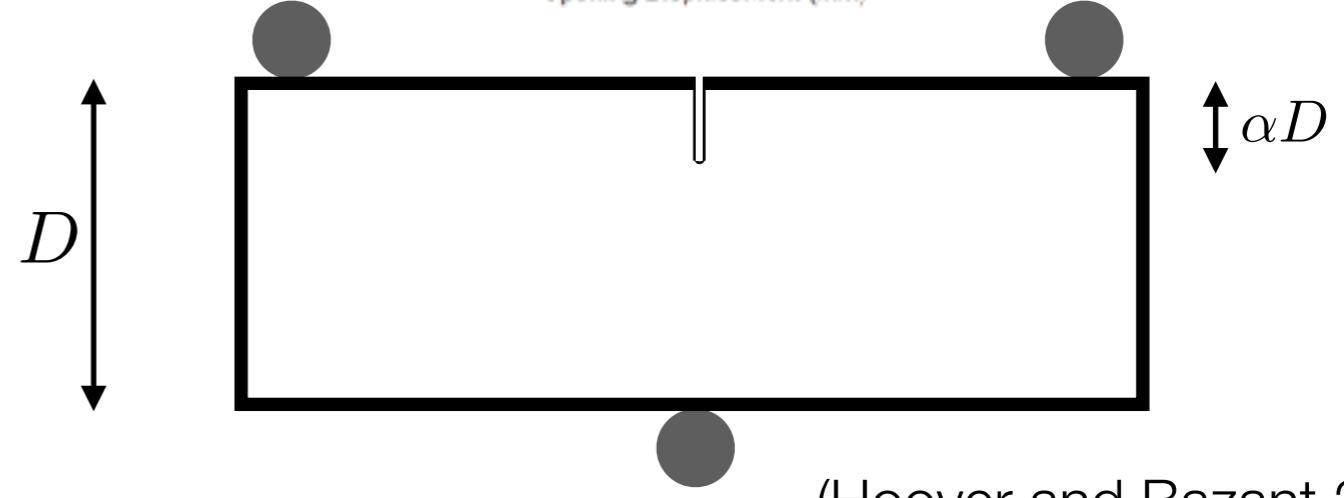
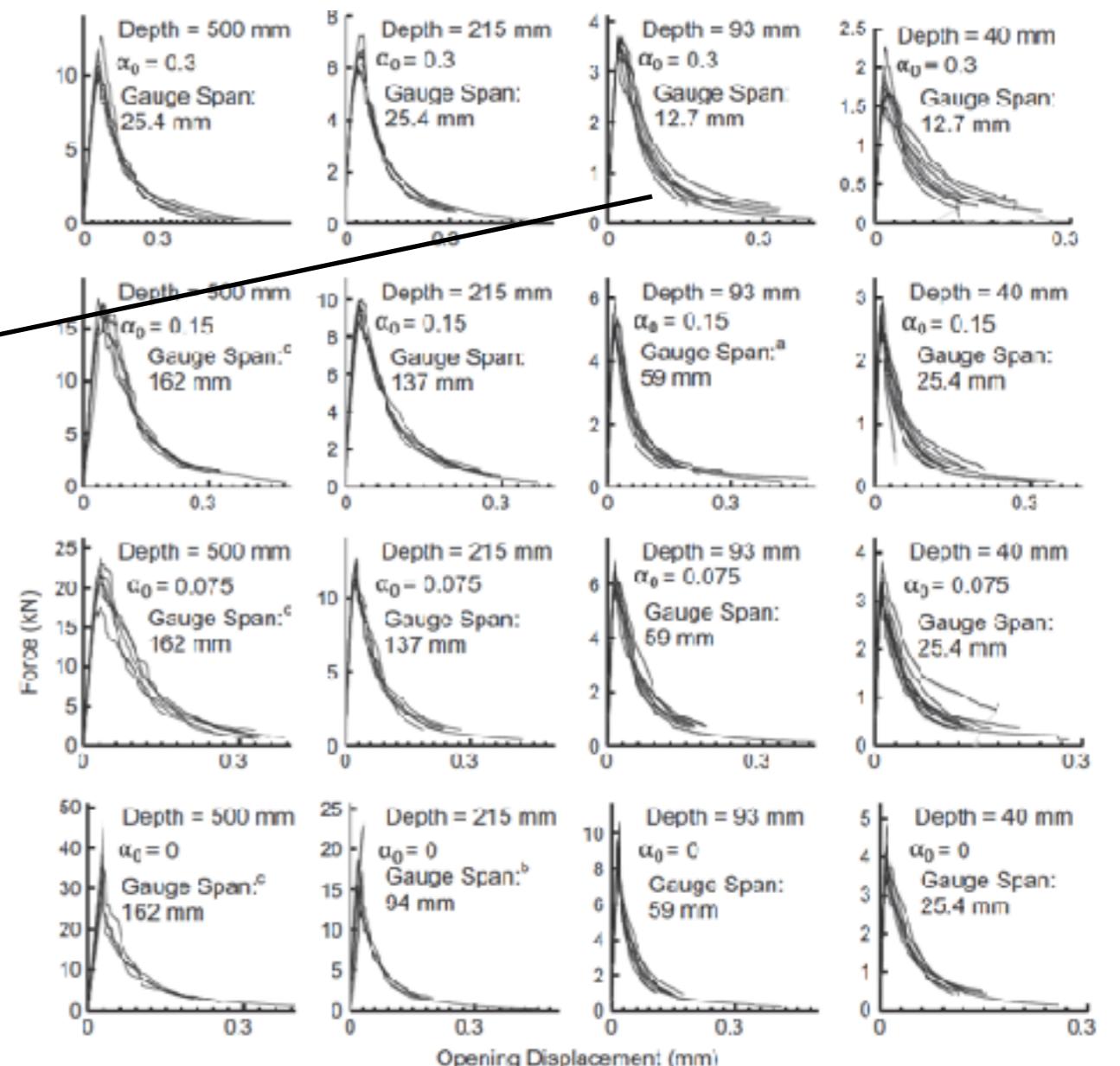
Notch width: 1.5 mm

$D = 40$  to 500 mm

# Three point bend tests -Concrete



$D = 40 \text{ to } 500 \text{ mm}$



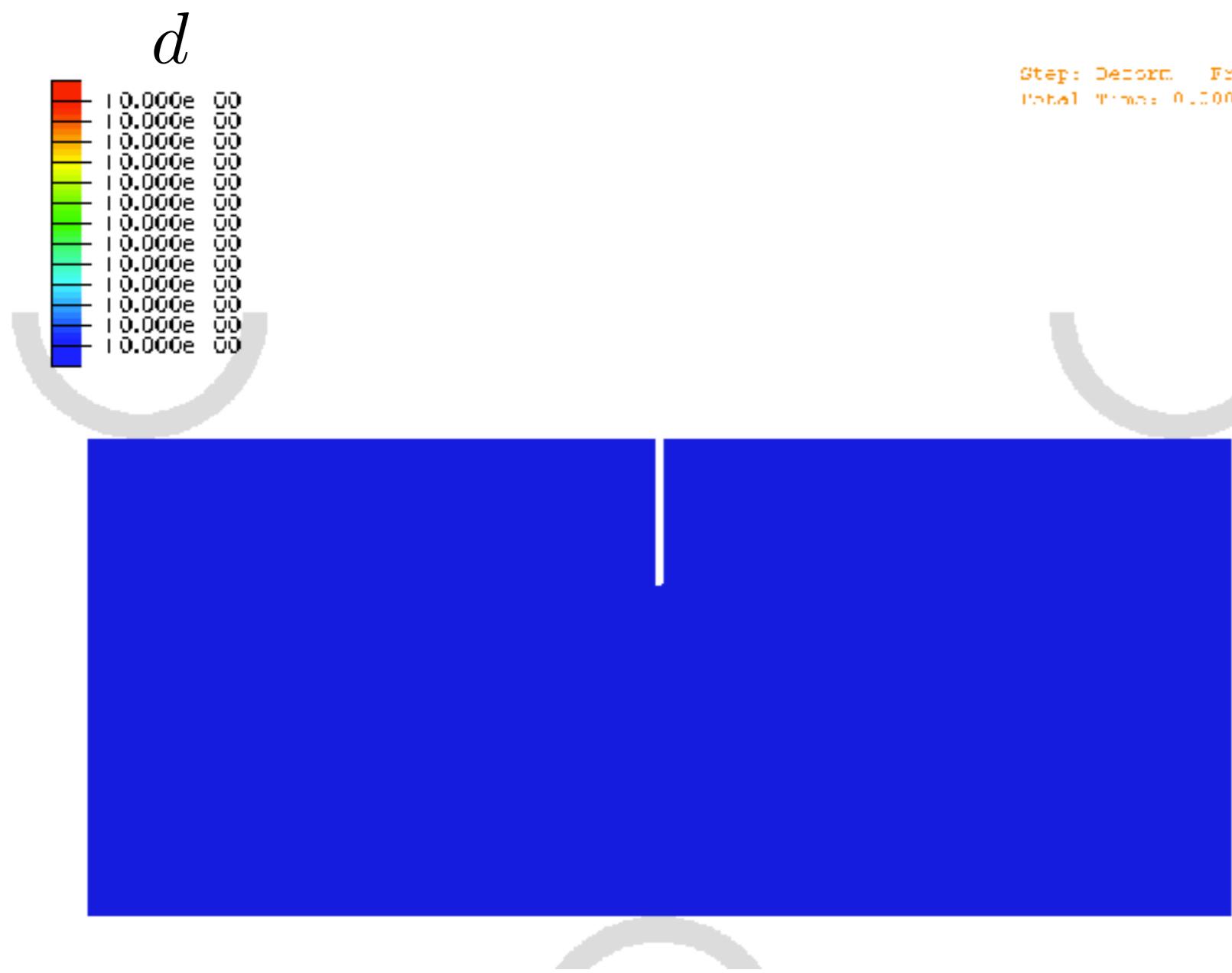
(Hoover and Bazant, 2013)

# Simulation

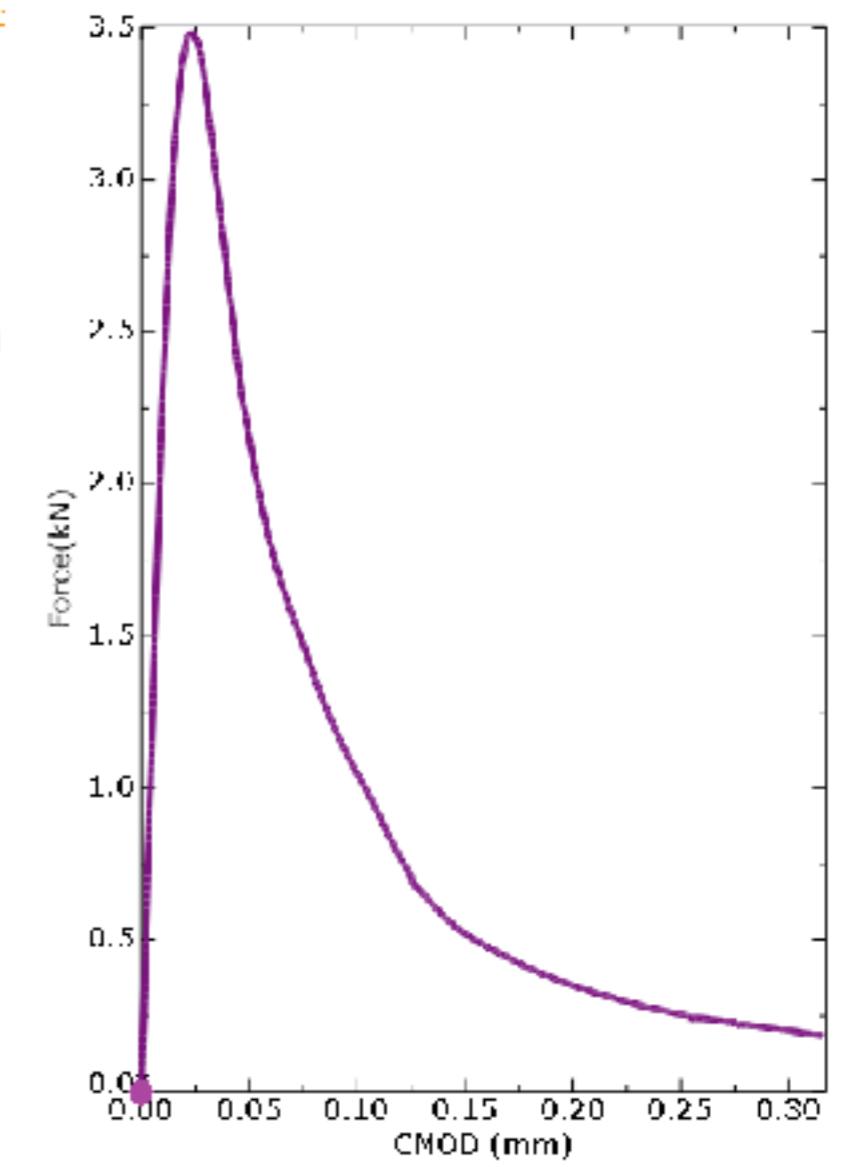
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$D = 93 \text{ mm}$

$\alpha = 0.3$



Displacements magnified 10x

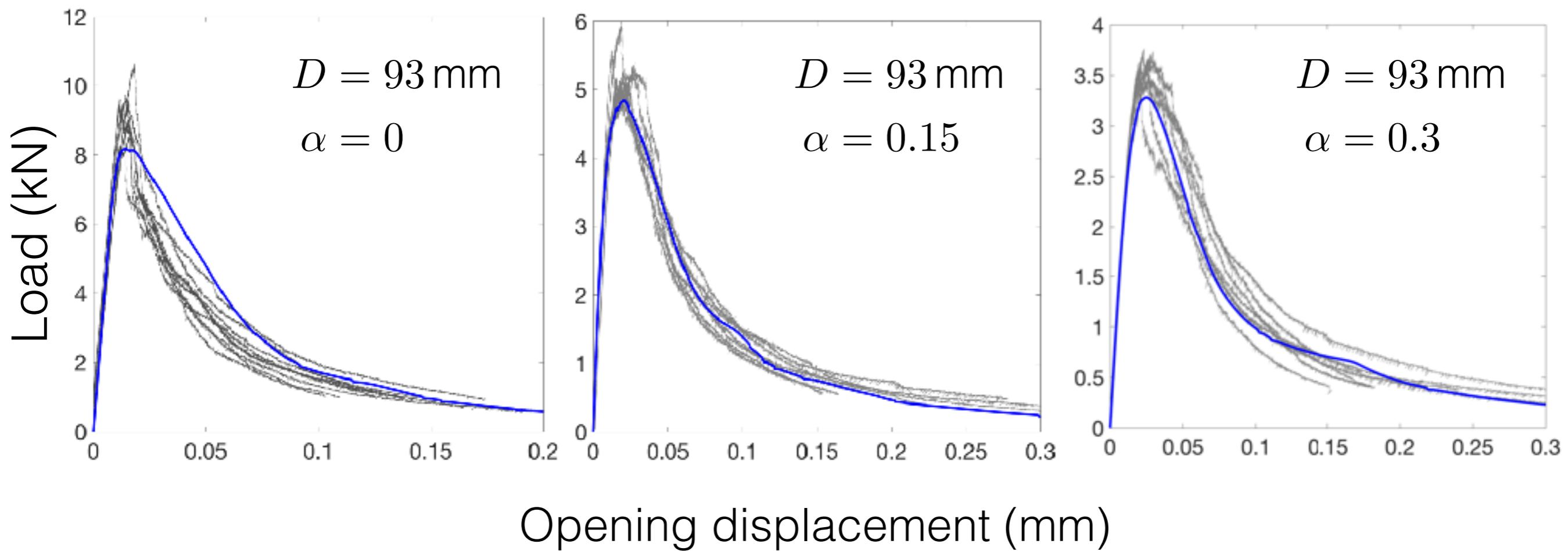


$\delta$

# Simulations vs. Experiments

— Experiments (Hoover and Bazant)

— Simulation (Our model)

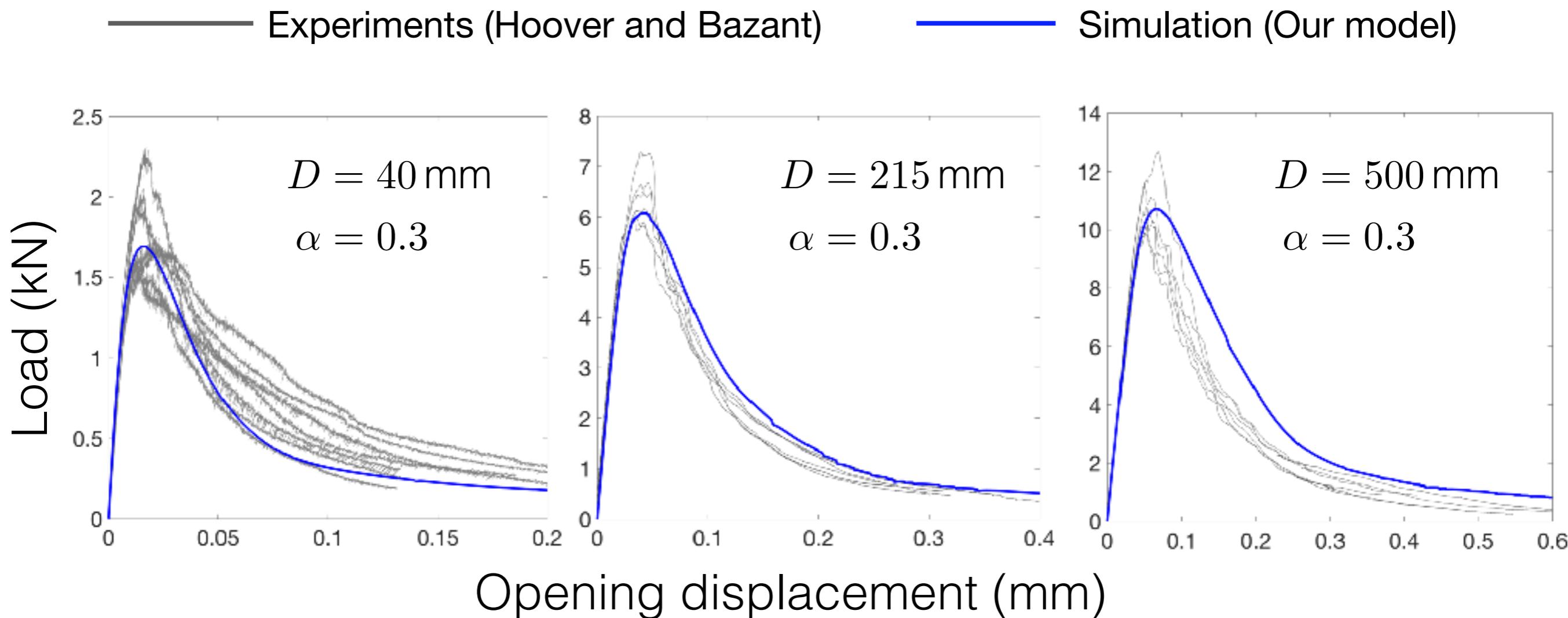


Opening displacement (mm)

Material Parameters

$E$	$\nu$	$S^c$	$\varkappa$	$\epsilon_{\text{crit}}^c$	$\psi_*$	$\ell$	$\zeta$
41	0.17	4.5	0.7	$4.4 \times 10^{-4}$	3.8	2	40
GPa	-	MPa	-	-	kJ/m <sup>3</sup>	mm	kPa-s

# Simulation vs Experiment



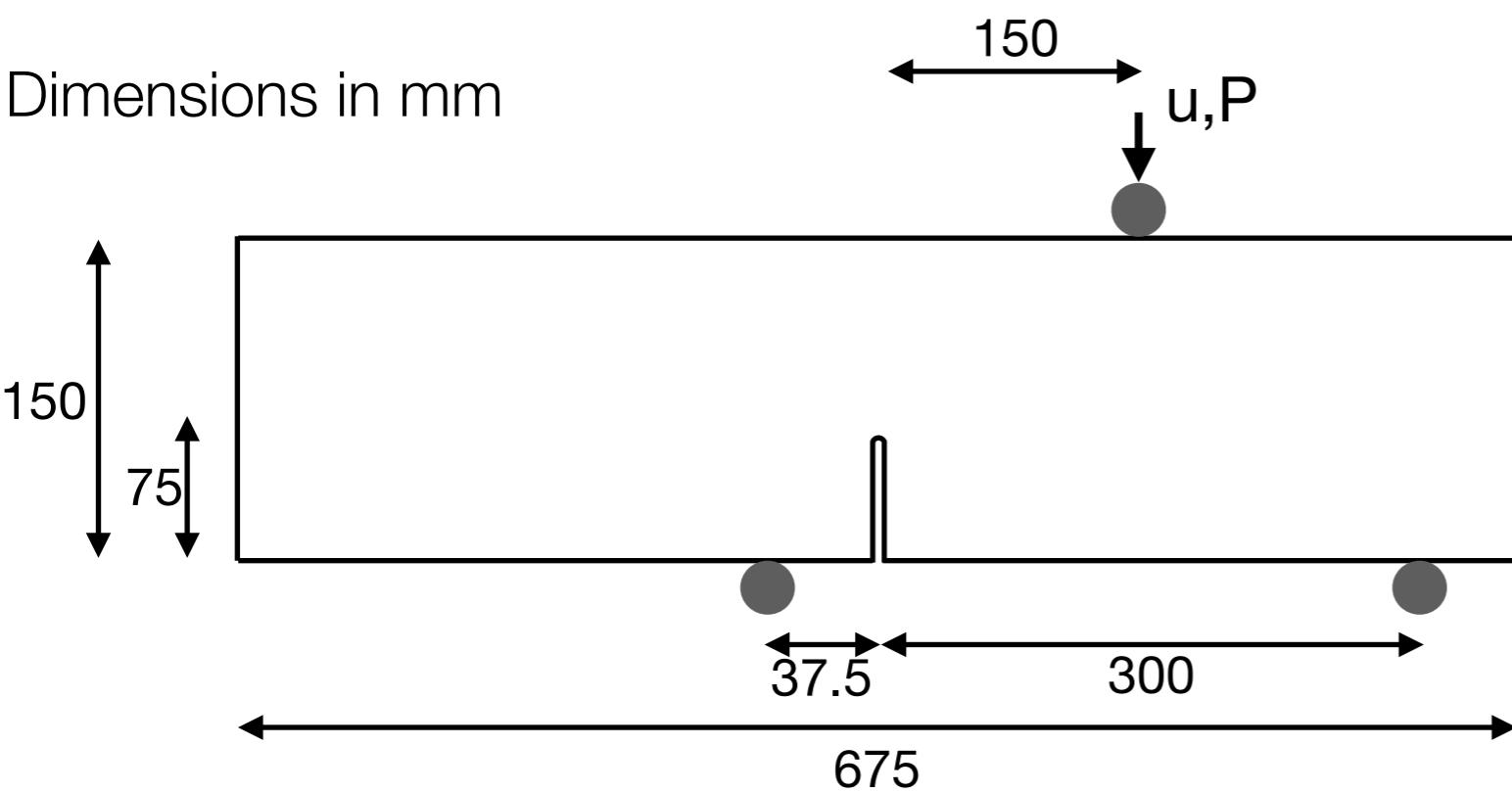
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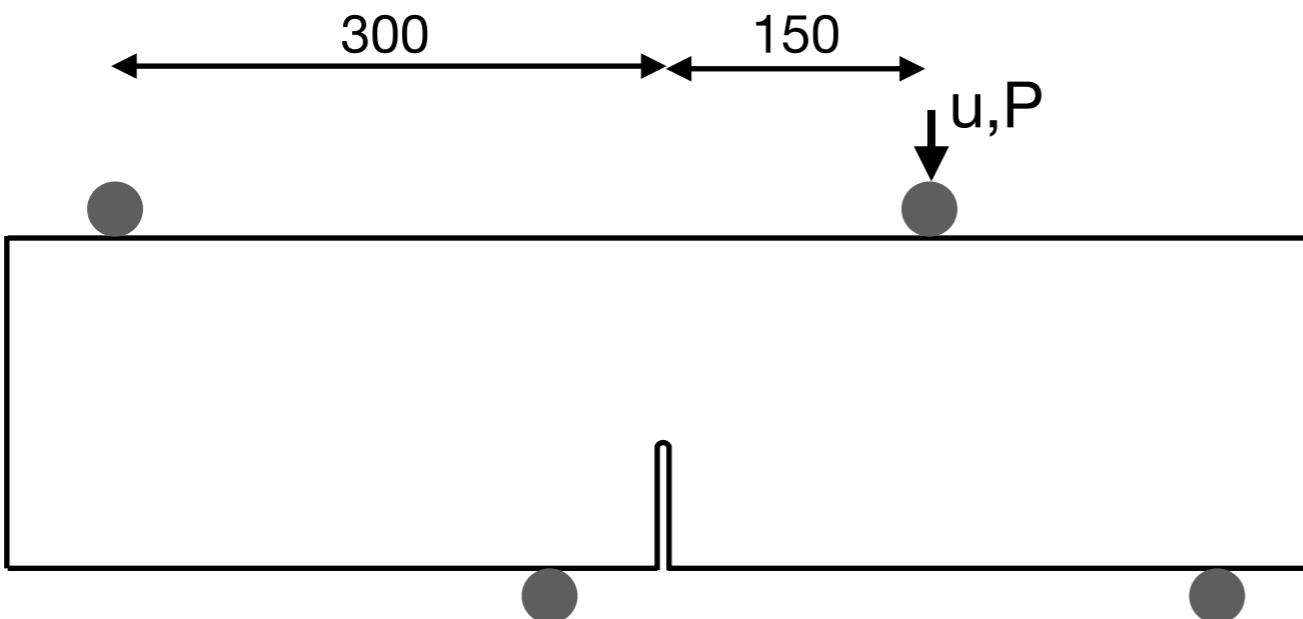
# Mixed-mode fracture tests

# Asymmetric bend tests

Dimensions in mm

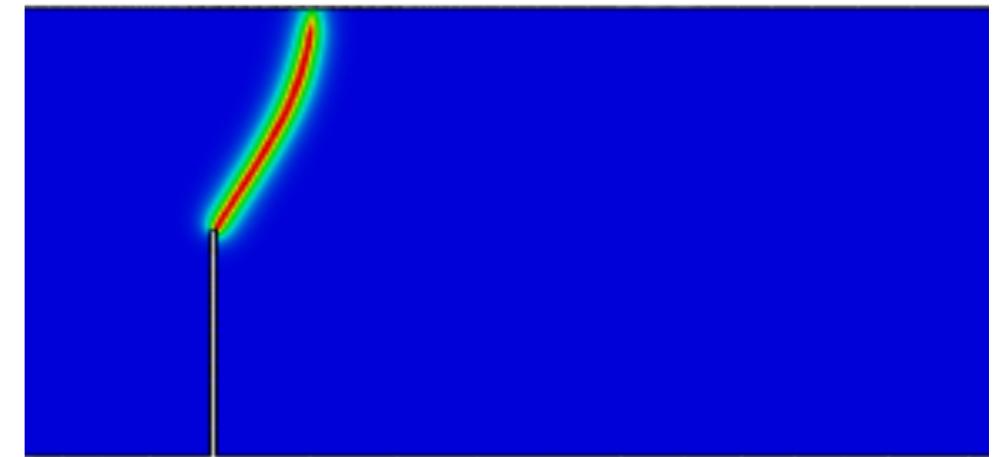


Notch width : 2 mm

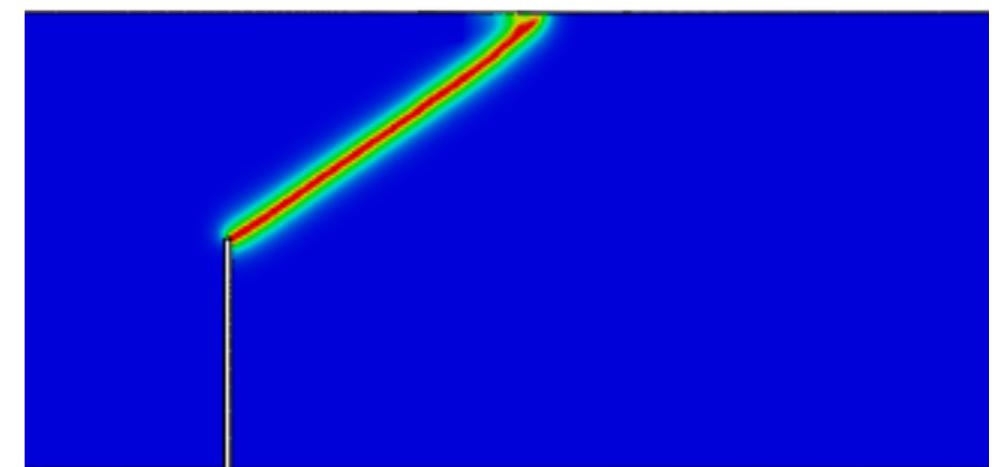


Thickness : 50

(Galvez et al, 1998)



Three-point bend :  
simulated crack path



Four-point bend :  
simulated crack path

# Comparison of predicted and measured crack paths

